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A general method for retrieving thermal deformation properties of microencapsulated phase change materials or other particulate inclusions in cementitious composites



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ABSTRACT

This study examined the effects of spherical core-shell particle inclusions, such as microencapsulated phase change materials (PCMs), on the thermal deformation behavior of cement-based composites. First, simulations of volumetric thermal deformation in representative microstructures were carried out, based on the finite element method (FEM), to predict the effective thermal deformation coefficient of the composites. Excellent agreement was found between the effective thermal deformation coefficient predicted by FEM and by the effective medium approximation (EMA) developed by Schapery (1968). Furthermore, the effective thermal deformation coefficient of cementitious composites with either microencapsulated PCM or quartz particulates was measured. The measured effective thermal deformation coefficients together with Schapery's model were used to retrieve the thermal deformation coefficients of the inclusions themselves. The thermal deformation coefficient of PCM microcapsules was estimated to be similar to that of the shell component due to partial filling of the microcapsules. The results show a means for (i) retrieving the thermal deformation properties of functional core-shell inclusions and (ii) for designing cementitious composites with PCMs which find use in the built environment and high-performance composites.

1. Introduction

In 2013, The American Society of Civil Engineers gave the road infrastructure in the United States a grade of "D", and estimated that \$67 billion is spent annually on the repair of deficient or damaged road pavements [1]. Substantial damage is caused to concrete pavements due to volume change that results from temperature change—caused by (i) cement hydration reactions at early ages, over the first 7 days following concrete placement, and (ii) ambient temperature change, at later ages (that results in fatigue damage) [2,3]. Microencapsulated phase change materials (PCMs) have been proposed as a means to mitigate thermal damage in concrete pavements [4,5]. Microencapsulated PCMs, a core-shell particulate, are thermal energy storage materials that can store and release latent heat associated with reversible phase transitions between the liquid and solid phases [6]. In concrete pavements, such storage and release of heat can be exploited to: (i) reduce early-age temperature rise and (ii) decrease the amplitude of diurnal temperature oscillations to reduce thermal fatigue damage [4,5].

PCM particulates with a median diameter on the order of 10 to 20 μ m are often produced by an interfacial polymerization process wherein a polymer shell (e.g., of melamine-formaldehyde) is used to encapsulate a core material (e.g., alkanes such as paraffin wax). To provide stress-relief over multiple phase change cycles, typically, the PCM micro-capsules are only partially filled—as a result, they contain some internal porosity [6]. Due to the presence of this internal porosity, and their small size, it is challenging to characterize the material properties of these core-shell structures. This is especially so in the

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Nomenclature		ϕ_n	volume fraction of material n in composite
		ρ	density, kg/m ³
С	material/stiffness tensor, GPa	σ	Cauchy stress tensor, GPa
D	diameter, μ m	ε	strain tensor
Ε	Young's modulus, GPa	ν	Poisson's ratio
G	shear modulus, GPa		
I	identity tensor	Subscripts	
Κ	bulk modulus, GPa		
L	unit cell length, μ m	с	refers to core material in composite
Μ	number of experimental measurements	c + s	refers to core-shell microcapsule
Ν	number of unit cells or number of constituent materials in	eff	refers to effective properties
	composite	j	refers to face <i>j</i> of unit cell
$\hat{\mathbf{n}}_i$	unit normal vector to face <i>j</i> of unit cell	ls	refers to limestone
Ť	temperature, °C	т	refers to matrix material in composite
T_{pc}	PCM melting temperature, °C	n	refers to constituent material n in composite
T_{ref}	reference/zero-strain temperature, °C	р	refers to inclusion
น้	displacement vector, m	q	refers to quartz
и	x-displacement, m	S	refers to shell material in composite
ν	y-displacement, m		
w	z-displacement, m	Superscrip	ots
w/c	water/cement ratio, mass basis		
		Т	denotes matrix/vector transpose
Greek syn	ıbols		
α	thermal deformation coefficient, $\mu \epsilon / {}^{\circ}C$		

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context of thermal deformation behavior when both the core and the shell would expand (or contract), albeit to different extents. This is an issue in applications such as concrete pavements, where it is important to know the thermal deformation coefficients of inclusions that are embedded in the cementitious matrix so as to quantify their influences on the volume stability of the overall solid.

The present study aims to assess the influences of PCM microcapsules on the effective thermal deformation coefficient of cementitious composites by complementary approaches including (i) finite element simulations of volumetric thermal deformation in representative microstructures, (ii) effective medium approximations, and (iii) measurements of linear thermal deformation of prismatic composite specimens. By identifying an effective medium approximation (EMA) capable of accurately estimating the effective thermal deformation coefficient of multicomponent composites consisting of a matrix and core-shell inclusions, a general approach is highlighted (i) for retrieving the thermal deformation coefficient of core-shell microcapsules or other particulate inclusions embedded in a continuous matrix and (ii) for designing cementitious composites with PCMs.

2. Background

2.1. Thermal deformation of solids

The constitutive law for a linearly elastic material considering thermal effects is given by [7],

$$\boldsymbol{\sigma} = \mathbf{C}: (\boldsymbol{\varepsilon} - \boldsymbol{\varepsilon}_T) \quad \text{or} \quad \sigma_{ij} = C_{ijkl} (\varepsilon_{kl} - \varepsilon_{T,kl}) \tag{1}$$

where e and e_T denote the total and thermal strain tensors, respectively, and **C** is the stiffness tensor. If the material is isotropic, the components of the stiffness tensor **C** can be expressed in terms of the material's elastic constants according to [8],

$$C_{ijkl} = \lambda \delta_{ij} \delta_{kl} + G(\delta_{ik} \delta_{jl} + \delta_{il} \delta_{jk})$$
⁽²⁾

where the Lamé parameter λ and shear modulus *G* are related to the Young's modulus *E* and Poisson's ratio ν according to [8],

$$\lambda = \frac{E\nu}{(1+\nu)(1-2\nu)} \quad \text{and} \quad G = \frac{E}{2(1+\nu)}.$$
 (3)

For an isotropic material, the thermal strain ε_T is related to the imposed temperature change ΔT according to [7],

$$\boldsymbol{\varepsilon}_T = (\alpha \Delta T) \mathbf{I} \quad \text{or} \quad \boldsymbol{\varepsilon}_{T,ij} = \alpha \Delta T \delta_{ij}$$
(4)

where α is the thermal deformation coefficient and ΔT is defined with respect to some reference or zero-strain temperature T_{ref} , i.e., $\Delta T = T - T_{ref}$ [7]. Note that in a homogeneous material that is not mechanically restrained, $\boldsymbol{\epsilon} = \boldsymbol{\epsilon}_T$ and the stress field is identically zero throughout the material. On the other hand, if it is fully restrained then $\boldsymbol{\epsilon} = 0$ and a stress is induced for $\Delta T \neq 0$.

2.2. Effective medium approximations

This study considers three simple effective medium approximations (EMAs) that can be applied to predict the effective thermal deformation coefficient α_{eff} of composites consisting of two or more constituents. The parallel model, also known as the rule-of-mixtures (ROM) [9], can be used to estimate the effective thermal deformation coefficient of a composite material with *N* components as a simple volume-weighted average over the constituent thermal deformation coefficients, i.e. [9],

$$\alpha_{eff} = \sum_{n=1}^{N} \phi_n \alpha_n \tag{5}$$

where ϕ_n and α_n are the volume fraction and thermal deformation coefficient of constituent material *n*, respectively. Turner [10] suggested that the ROM be adjusted to weigh each component *n* by their respective volume fraction ϕ_n and bulk modulus K_n , such that

$$\alpha_{eff} = \frac{\sum_{n=1}^{N} \phi_n K_n \alpha_n}{\sum_{n=1}^{N} \phi_n K_n}.$$
(6)

Schapery [11] derived an EMA which gave upper and lower bounds for the effective thermal deformation coefficient α_{eff} of composites with *N* components based on energy conservation considerations. In this case, α_{eff} was expressed as an average of upper and lower bounds such that,

$$\alpha_{eff} = \overline{\alpha} + \left(\frac{\overline{K\alpha}}{\overline{K}} - \overline{\alpha}\right) \frac{\frac{1}{K_L} - \frac{1}{K_{eff}}}{\frac{1}{K_L} - \frac{1}{\overline{K}}} \pm \Delta\alpha.$$
(7)

Here, the overline denotes a volume-weighted average over the constituents, i.e. [11],

$$\overline{\alpha} = \sum_{n=1}^{N} \phi_n \alpha_n, \quad \overline{K} = \sum_{n=1}^{N} \phi_n K_n, \quad \text{and} \quad \overline{K\alpha} = \sum_{n=1}^{N} \phi_n K_n \alpha_n.$$
(8)

In addition, K_L is given by,

$$K_L = \left(\sum_{n=1}^N \frac{\phi_n}{K_n}\right)^{-1} \tag{9}$$

and the effective bulk modulus K_{eff} can be estimated as the average of K_L and \overline{K} , i.e., $K_{eff} = (K_L + \overline{K})/2$. Finally, the deviation $\Delta \alpha$ in α_{eff} from the average was expressed as [11],

$$\Delta \alpha = \frac{\left(\frac{1}{K_{eff}} - \frac{1}{\overline{K}}\right)^{1/2} \left(\frac{1}{\overline{K_L}} - \frac{1}{\overline{K_{eff}}}\right)^{1/2}}{\frac{1}{\overline{K_L}} - \frac{1}{\overline{K}}} \times \left[\left(\overline{K\alpha^2} - \frac{(\overline{K\alpha})^2}{\overline{K}}\right) \left(\frac{1}{\overline{K_L}} - \frac{1}{\overline{K}}\right) - \left(\frac{\overline{K\alpha}}{\overline{K}} - \overline{\alpha}\right)^2 \right]^{1/2}.$$
(10)

Note that each of the aforementioned EMAs was developed for a linearly elastic composite featuring isotropic constituent materials with arbitrary geometry. The effective thermal deformation coefficient predicted by each EMA depends only on the volume fractions and thermomechanical properties of the constituent materials but is independent of their spatial distribution. They can also be extended to a composite made of any number of constituents. As such, these EMAs are easily applied to cementitious and other composite materials with more than one type of inclusion, including both fine aggregates (e.g., quartz sand) and soft inclusions (e.g., microencapsulated PCM), as well as coarse aggregates that would be present in a typical concrete pavement. In addition, several other EMAs have been developed specifically for two-component composites—further details can be found in Ref. [12].

3. Materials and methods

3.1. Materials

An ASTM C150 [13] compliant Type I/II ordinary portland cement (OPC) was mixed with deionized (DI) water to prepare cement pastes (matrix only) and mortars (matrix + inclusions) in accordance with ASTM C192 [14]. The OPC had a nominal mass-based mineralogical composition of: 56.5% Ca₃SiO₅, 18.0% Ca₂SiO₄, 11.4% Ca₄Al₂Fe₂O₁₀, 6.3% Ca₃Al₂O₆, 4.6% CaCO₃, and 1.1% CaSO₄ ·2H₂O. ASTM C778 [15] compliant graded quartz sand and microencapsulated PCM inclusions (MPCM24D, Microtek Laboratories) were used as inclusions within the cement mortars. The microencapsulated PCMs consisted of a paraffin core encapsulated within a melamine-formaldehyde (MF) shell. The microencapsulated PCMs were received in the form of dry powders. The corresponding peak melting temperature and enthalpy of phase change of microencapsulated PCMs were 27.8°C and 161.2 ± 0.5 kJ/kg representing the average value over three melting and solidification cycles.

Cementitious mortars were prepared with various volume fractions (i.e., dosages) of microencapsulated PCM and/or quartz inclusions at a water-to-cement ratio (w/c, mass basis) of 0.45. For mortars containing microencapsulated PCM inclusions only, the inclusions were dosed for three different volume fractions, namely, 5, 10 and 20 vol.%. For mortars containing quartz inclusions only, the quartz dosages were 10, 20, and 50 vol.%. For mortars containing mixed inclusions, the total inclusion volume fraction was fixed at 50 vol.%, where the microencapsulated PCM inclusions comprised 10, 15, or 20 vol.%. The microencapsulated PCMs were mixed with the anhydrous OPC by hand

prior to the addition of DI water to ensure random and uniform distribution in the mortar. To enhance the fluidity of the fresh mixtures, a commercially available water-reducing admixture (MasterGlenium 7500, BASF Corporation) was added at a dosage on the order of 0-to-1.5 wt.% by mass of cement, depending on the type and dosage of inclusions present.

3.2. Experimental methods

Thermal deformation coefficient measurements were carried out using prismatic specimens with various mixture proportions, as described above. The specimens were cast in 2.54 cm x 28.50 cm molds in accordance with ASTM C157 [16] and cured under 100% relative humidity for the first 24 h at 25°C. Following demolding after 24 h, the specimens were sealed with aluminum tape and cured in sealed bags at 25°C for 28 days. Then, the length of each specimen was measured at 25°C and the specimens were transferred to an environmental chamber (KB024-DA, Darwin Chambers Company) at 45°C, and stored for 2 h until they reached thermal equilibrium. The fractional length change (i.e., the linear thermal strain) $\Delta L/L_0$ due to temperature change $\Delta T = 45^{\circ}$ C-25°C was measured with a length comparator, as illustrated in Fig. 1. Then, the thermal deformation coefficient of the specimens was calculated according to,

$$\alpha_{eff} = \frac{\Delta L}{L_0 \Delta T}.$$
(11)

In addition, elastic thermal strain within the specimens was verified by also calculating α_{eff} based on a temperature change from 5°C to 45°C and verifying that the measured α_{eff} was independent of the imposed temperature change. It was also confirmed that the specimens recovered their initial length when returned to their initial temperature of 25°C. Such elastic stress-strain behavior implies that the thermal deformation coefficient of cementitious composites would remain constant across the range of diurnal temperature variations that would be experienced by a concrete pavement. However, when the concrete's temperature falls below 0° C, its thermomechanical behavior is



Fig. 1. Photograph of the experimental setup used to measure the effective thermal deformation coefficient of cementitious composites containing microencapsulated PCMs and/or quartz sand inclusions.

complicated by melting and freezing of water within its pores [17] and thus cannot be treated as simple elastic deformation.

4. Analysis

4.1. Schematic and assumptions

Fig. 2 illustrates the computational cubic unit cells of length *L* utilized in this study, along with the associated coordinate system. Free thermal deformation was simulated numerically in domains with ordered monodisperse packing arrangements, namely (a) body-centered cubic (BCC), (b) simple cubic (SC), or (c) face-centered cubic (FCC) or in domains with randomly distributed (d) monodisperse or (e) polydisperse microcapsules. The core and shell volume fractions ϕ_c and ϕ_s can be expressed in terms of the average core and shell diameters $\overline{D_c}$ and $\overline{D_s}$ and the unit cell length *L* according to,

$$\phi_c = \frac{N_p \pi \overline{D}_c^3}{6L^3} \quad \text{and} \quad \phi_s = \frac{N_p \pi (\overline{D}_s^3 - \overline{D}_c^3)}{6L^3} \tag{12}$$

where N_p is the number of core-shell particles contained within the unit cell.

A stochastic packing algorithm [18] was used to generate the size and location of randomly distributed monodisperse and polydisperse microcapsules within unit cells of edge length $L = 75 \ \mu\text{m}$ (Fig. 2d–e). The algorithm placed microcapsules at random locations within the unit cell until the desired core volume fraction ϕ_c was achieved within 0.5%. It ensured that the minimum centroidal distance between two sphere centers C_D was greater than the sum of their radii $r_1 + r_2$ [18]. The packing algorithm considered a particle size distribution with average shell diameter $\overline{D_s} = 18 \ \mu\text{m}$ as well as 10th and 95th percentile shell diameters equal to 9 $\ \mu\text{m}$ and 33 $\ \mu\text{m}$, respectively [18]. All microcapsules had a shell thickness of 1 $\ \mu\text{m}$, i.e., $(D_s - D_c)/2 = 1$ μ m [18]. Previously, we used the same microstructures to predict the effective thermal conductivity [19] and elastic moduli [20] of threecomponent composites. The size and location of the microcapsules can be found in supplementary material.

To make the problem mathematically tractable, it was assumed that (i) all materials were linearly elastic and isotropic, (ii) body forces were negligible, and (iii) continuous contact was maintained at the material interfaces, i.e., no sliding or gapping was allowed.

4.2. Governing equations and boundary conditions

The stress field in each component was governed by the steady-state differential equilibrium equation [8],

$$\nabla \cdot \boldsymbol{\sigma}_n = 0$$
 (13)

where σ_n is the local stress tensor in component *n* referring to the core (subscript *c*), shell (subscript *s*), or matrix (subscript *m*). The stress σ_n and strain ε_n tensors were related according to the constitutive law given by Eq. (1). Here, the temperature rise ΔT was imposed by fixing the temperature at each face of the cube at $T = T_{ref} + \Delta T$ such that solving the steady-state heat diffusion equation resulted in a spatially uniform temperature *T* throughout the domain. Additionally, the strain-displacement relation in each component was given by [8],

$$\boldsymbol{\varepsilon}_n = \frac{1}{2} \left[\nabla \mathbf{u}_n + (\nabla \mathbf{u}_n)^T \right]$$
(14)

where $u_n = [u_n, v_n, w_n]^T$ is the displacement vector in component *n*.

In order to fully define the problem, boundary conditions on each of the cube's six faces, denoted by index *j*, were prescribed to represent free volumetric thermal deformation. For ordered packing arrangements (Fig. 2a–c), the faces at x = 0 (j = 1), y = 0 (j = 2), and z = 0 (j = 3) were fixed by virtue of symmetry, i.e.,



Fig. 2. Schematic of computational cells with various particle size distributions and packing arrangements used in numerical simulations of free thermal deformation in three-component composites consisting of spherical microcapsules in a continuous matrix, namely, (a) body-centered cubic (BCC), (b) simple cubic (SC), (c) face-centered cubic (FCC), (d) randomly distributed monodisperse microcapsules, and (e) randomly distributed polydisperse microcapsules.

$$\mathbf{u}_n \cdot \hat{\mathbf{n}}_j = 0 \quad \text{for} \quad j = 1, 2, \text{ or} 3 \tag{15}$$

where $\hat{\mathbf{n}}_{j}$ denotes the unit normal vector to face *j*. The remaining faces were allowed to expand freely. As such, the traction force on these faces vanished [8],

$$\boldsymbol{\sigma}_n \cdot \hat{\mathbf{n}}_j = 0 \quad \text{for} \quad j = 4, \, 5, \, \text{or6.} \tag{16}$$

Moreover, for unit cells with randomly distributed microcapsules (Fig. 2d–e), all six faces were allowed to expand freely, i.e.,

$$\sigma_n \cdot \hat{\mathbf{n}}_j = 0 \quad \text{for} \quad j = 1, 2, ..., \text{or6.}$$
 (17)

4.3. Data processing

Solving the governing Eqs. (1), (13) and (14) along with their corresponding boundary conditions yields the displacement field $\mathbf{u}_n(x,y,z)$ in each component of the composite volume initially at V_0 . Then, the corresponding change in volume ΔV of the deformed body for a temperature change of ΔT was used to compute the effective thermal deformation coefficient α_{eff} (in $\mu e/^{\circ}$ C, neglecting higher-order strain terms) according to [7],

$$\alpha_{eff} = \frac{1}{3} \frac{\Delta V}{V_0 \Delta T}.$$
(18)

4.4. Method of solution

The governing Eqs. (1), (13), and (14) along with the corresponding boundary conditions [Eqs. (15)– (17)] were solved using the finite element method with the commercially available finite element solver COMSOL Multiphysics^{*}. Computation was performed on a single CPU with two 2.6 GHz processors and 8 GB RAM. Numerical convergence was verified such that the predicted value of α_{eff} did not change by more than 0.5% when the minimum element size was decreased by a factor of 2. Numerical convergence was reached using a minimum element size of 0.2 μ m and a maximum element growth rate of 1.5. The number of finite elements in the computational domain ranged from 66,252 to 534,108. In addition, it was verified that the predicted α_{eff} was independent of the imposed temperature difference ΔT for 5°C $< \Delta T$ < 30°C.

5. Results and discussion

5.1. Numerical simulations

This section uses numerical simulations of free thermal deformation to elucidate the effect of geometric parameters as well as constituent material properties on the effective thermal deformation coefficient α_{eff} of three-component composites consisting of spherical microcapsules in a continuous matrix. Table 1 outlines the baseline case values of thermal deformation coefficient α , Young's modulus *E*, Poisson's ratio ν , and bulk modulus *K* used in the simulations. These properties were chosen to represent a composite consisting of microencapsulated PCM inclusions in a cementitious matrix [20–23]. Note that the bulk modulus *K* is related to the Young's modulus *E* and Poisson's ratio ν according to [8],

$$K = \frac{E}{3(1 - 2\nu)}.$$
 (19)

5.1.1. Effect of computational domain size

Fig. 3 plots the numerically predicted effective thermal deformation coefficient a_{eff} as a function of the total number of simulated BCC, FCC, or SC unit cells *N* in the cubic computational domain for N = 1, 8 (2 × 2 × 2), or 27 (3 × 3 × 3). Here, unit cells with three sets of core and shell volume fractions ϕ_c and ϕ_s were simulated. Fig. 3 establishes

that α_{eff} was independent of the number of unit cells simulated. The predicted α_{eff} was also nearly identical for each ordered packing arrangement (BCC, FCC, or SC). Indeed, the maximum relative difference between α_{eff} for any two different domain sizes or packing arrangements was less than 2%. Note that these small variations in α_{eff} were expected due to the absence of periodicity in the imposed boundary conditions. Based on this result, a domain consisting of a single unit cell with BCC packing was used for all further simulations of domains featuring ordered microcapsules.

5.1.2. Effect of core and shell volume fractions

Fig. 4 plots the numerically predicted effective thermal deformation coefficient α_{eff} as a function of the core-shell volume fraction ϕ_c $+_s = \phi_c + \phi_s$ ranging from 0 to 0.5. The thermomechanical properties of each constituent material were those of the baseline case (Table 1). Here, the ratio of core to core-shell volume fractions ϕ_c/ϕ_{c+s} was held constant and equal to either 0.5 or 0.85. The corresponding core and shell volume fractions ϕ_c and ϕ_s were imposed by fixing either (i) the core diameter D_c , (ii) the shell diameter D_s , or (iii) the unit cell length L in Eq. (12). Fig. 4 shows that the effective thermal deformation coefficient α_{eff} increased linearly with increasing core-shell volume fraction ϕ_{c+s} . This was due to the fact that both the core thermal deformation coefficient α_s were larger than that of the matrix α_m . In addition, for given core and shell volume fractions, α_{eff} was the same regardless of which geometric parameter D_c , D_s , or L was fixed.

Moreover, Fig. 4 also shows predictions from (i) the ROM or parallel model [Eq. (5)], (ii) Turner's model [Eq. (6)], and (iii) the average of the upper and lower bounds of Schapery's model [Eq. (7)]. Excellent agreement was found between the numerical predictions of α_{eff} and predictions from Schapery's model. The ROM and Turner's model overestimated and underestimated the numerical predictions, respectively.

5.1.3. Effect of size and spatial distributions

Table 2 reports the effective thermal deformation coefficient α_{eff} predicted numerically using computational domains with different core and shell volume fractions ϕ_c and ϕ_s and with either ordered monodisperse or randomly distributed monodisperse or polydisperse microcapsules. Note that very similar values of α_{eff} were obtained for Cases $1-3(\phi_c \approx 0.1, \phi_s \approx 0.04)$ and also for Cases $4-5(\phi_c \approx 0.2, \phi_s \approx 0.05)$. Thus, for a given ϕ_c and ϕ_s , α_{eff} did not depend on the packing arrangement (i.e., ordered or random) or microcapsule size distribution (i.e., monodisperse or polydisperse). In other words, a single unit cell with BCC packing was representative of the thermal elastic behavior of cells with randomly distributed monodisperse or polydisperse microcapsules. In light of these results, a computational domain consisting of a single unit cell with BCC packing was utilized for the remainder of this study.

Moreover, predictions from Schapery's model [Eq. (7)] were again in excellent agreement with the numerically predicted α_{eff} and differed by less than 2% for all cases considered in Table 2.

5.1.4. Effect of constituent thermal deformation coefficients

Fig. 5 plots the numerically predicted effective thermal deformation

Table 1

Baseline case values of thermal deformation coefficient α , Young's modulus E, Poisson's ratio ν , and bulk modulus K of the core, shell, and matrix materials used in numerical thermal deformation simulations.

Material	Subscript	α (με/°C)	E (GPa)	ν	K (GPa)	Ref.
Core	c	109	0.056	0.499	9.3	[20,21]
Shell	s	50	6.3	0.34	6.6	[20,22]
Matrix	m	11	22.1	0.15	10	[23]



Fig. 3. Effective thermal deformation coefficient α_{eff} of three-component composites consisting of spherical microcapsules in a continuous matrix predicted numerically as a function of the number *N* of BCC, FCC, or SC unit cells in the cubic computational domain. The thermomechanical properties of the core, shell, and matrix materials are listed in Table 1.



Fig. 4. Numerically predicted effective thermal deformation coefficient a_{eff} as a function of the core-shell volume fraction $\phi_{c+s} = \phi_c + \phi_s$ for the baseline case (Table 1). Here, the ratio ϕ_c/ϕ_{c+s} was held constant and equal to 0.5 or 0.85 and the corresponding core and shell volume fractions ϕ_c and ϕ_s were imposed by fixing either (i) the core diameter D_c , (ii) the shell diameter D_s or (iii) the unit cell length *L*.

coefficient α_{eff} as a function of (a) the core thermal deformation coefficient α_c , (b) the shell thermal deformation coefficient α_s , and (c) the matrix thermal deformation coefficient α_m ranging from 0 to 500 $\mu e / ^{\circ}$ C for core volume fraction $\phi_c = 0.2$ and shell volume fraction $\phi_s =$ 0.15. Each plot shows two different sets of values α_c , α_s , or α_m between 5 and 400 $\mu e / ^{\circ}$ C in an effort to explore a wide range of variation in constituent thermal deformation coefficients. Fig. 5 shows that α_{eff} increased linearly with each constituent's thermal deformation coefficient.

Moreover, Fig. 5 shows predictions by the ROM, Turner, and Schapery models. Here also, excellent agreement was observed between the Schapery model and the numerical predictions over the wide range of constituent thermal deformation coefficients considered, with a relative error not exceeding 3%.

5.2. Experimental measurements and property retrieval

This section presents a general method to retrieve the thermal deformation coefficient of particulate inclusions that are difficult to measure directly by combining Schapery's model [Eq. (7)], previously validated numerically, with the measured effective thermal deformation coefficient. Here, the thermal deformation coefficient α_p of the inclusions was retrieved by least-square fitting the experimentally measured effective thermal deformation coefficient for M different inclusion volume fractions ϕ_i to Schapery's model by minimizing the sum-of-squares error δ given by,

$$\delta = \sum_{i=1}^{M} \left[\alpha_{eff,exp}(\phi_i) - \alpha_{eff,Schapery}(\phi_i) \right]^2.$$
(20)

5.2.1. Validation

The suggested method for retrieving the inclusion thermal deformation coefficient was validated by demonstrating its use on experimental data presented by Walker et al. [24] for cement pastes with crushed limestone inclusions with volume fraction ϕ_{ls} ranging from 0 to 0.6. Additionally, the authors directly measured the thermal deformation coefficient of the cement paste alone as $\alpha_m = 9.72 \, \mu \epsilon / {}^{\circ}$ C, and that of the limestone as $\alpha_{ls} = 4.4 \ \mu \epsilon / ^{\circ} C$ by sawing specimens from the parent stone [24]. Here, the elastic modulus and Poisson's ratio of the limestone were taken as 31 GPa and 0.25, respectively [25]. Fig. 6 plots the experimentally measured effective thermal deformation coefficient α_{eff} as a function of limestone volume fraction ϕ_{ls} [24]. The error bars correspond to an uncertainty of \pm 5%. Fig. 6 also shows the best fit obtained with the Schapery model, corresponding to a retrieved value of $\alpha_{ls} = 4.3 \,\mu \epsilon/^{\circ}$ C. This value of α_{ls} agrees very well with that measured directly by the authors, thus demonstrating that our suggested approach can be used to obtain accurate estimates of inclusion thermal expansion coefficients.

5.2.2. Thermal deformation coefficient of PCM microcapsules

Fig. 7a plots the experimentally measured effective thermal deformation coefficient α_{eff} of cement paste with microencapsulated PCM

Table 2

Numerically predicted effective thermal deformation coefficient α_{eff} of composites consisting of ordered monodisperse or randomly distributed monodisperse or polydisperse core-shell microcapsules in a continuous matrix for the baseline case (Table 1).

Case	Packing	Size distribution	N_p	L (μm)	ϕ_c	ϕ_s	α_{eff} (µ ε /°C)	α _{eff} (με/°C)	% Error
							Numerical	Schapery [Eq. (7)]	
1	BCC	Monodisperse	2	22.2	0.096	0.041	21.2	21.2	0
2	Random	Monodisperse	19	75	0.097	0.041	21.0	21.3	1.5
3	Random	Polydisperse	22	75	0.095	0.041	20.9	21.1	1.1
4	BCC	Monodisperse	2	17.4	0.2	0.046	31.3	31.2	0.2
5	Random	Polydisperse	38	75	0.2	0.046	31.7	31.2	1.4



Fig. 5. Numerically predicted effective thermal deformation coefficient α_{eff} as a function of (a) core thermal deformation coefficient α_c , (b) shell thermal deformation coefficient α_s , or (c) matrix thermal deformation coefficient α_m ranging from 0 to 500 $\mu e/^{\circ}$ C. The core and shell volume fractions were $\phi_c = 0.2$ and $\phi_s = 0.15$.



Fig. 6. Effective thermal deformation coefficient α_{eff} of cement pastes with crushed limestone inclusions as a function of limestone volume fraction ϕ_{ls} ranging from 0 to 0.6 measured by Walker et al. [24] and predicted by Schapery's model using the retrieved value of $\alpha_{ls} = 4.3 \ \mu \epsilon / {}^{\circ}$ C.

specimens as a function of microencapsulated PCM volume fraction ϕ_{c}_{+s} ranging from 0 to 0.3. The error bars correspond to one standard deviation or 68% confidence interval of three measurements. Fig. 7a shows that α_{eff} slightly increased with increasing ϕ_{c+s} , confirming that the thermal deformation coefficient of the PCM microcapsules was indeed larger than that of the cementitious matrix. The latter was measured to be $\alpha_m = 14.1 \ \mu \varepsilon \rho^\circ C$, corresponding to $\phi_{c+s} = 0$. The thermal deformation coefficient α_{c+s} of the PCM microcapsules was retrieved by least-square fitting the experimental measurements of α_{eff} with Schapery's model, as outlined previously. In this case, the retrieved value of α_{c+s} was 42 $\mu \varepsilon \rho^\circ C$. Interestingly, this value was similar to the thermal deformation coefficient of the MF shell, reported in the literature as $\alpha_s = 50 \ \mu \varepsilon \rho^\circ C$ [22].

The PCM microencapsulation process is often carried out at elevated temperatures around 100°C [6]. During subsequent cooling, the paraffinous core contracts more than the shell, i.e., $\alpha_c > > \alpha_s$ (see Table 1), leaving some empty space in the PCM microcapsules at room temperature. Then, upon subsequent heating, the thermal deformation coefficient α_c of the core material has negligible impact on the thermal deformation coefficient α_{c+s} of the core-shell microcapsule, as the core is allowed to expand freely without exerting any stress on the shell. Therefore, the thermal deformation coefficient of the PCM microcapsule α_{c+s} is expected to be similar to that of the shell material for temperatures below 100°C.



Fig. 7. Experimentally measured thermal deformation coefficient a_{eff} of cement pastes containing (a) microencapsulated PCM with ϕ_{c+s} ranging from 0 to 0.25, (b) quartz sand with ϕ_q ranging from 0 to 0.6, or (c) both microencapsulated PCM and quartz sand with ϕ_{c+s} ranging from 0 to 0.25 and $\phi_q + \phi_{c+s} = 0.5$.

5.2.3. Thermal deformation coefficient of quartz sand inclusions

Fig. 7b plots the experimentally measured effective thermal deformation coefficient α_{eff} of cement mortar (i.e., cement paste with quartz sand inclusions) as a function of quartz inclusion volume fraction ϕ_q ranging from 0 to 0.5. In this case, the low thermal deformation

coefficient of the quartz sand caused α_{eff} to decrease with increasing quartz volume fraction ϕ_q . Here again, the thermal deformation coefficient of the quartz inclusions α_q was determined by least-square fitting the experimental measurements to the Schapery model. The elastic modulus E_q and Poisson's ratio ν_q of quartz were taken, from the literature, as 73 GPa and 0.17, respectively [26]. Here, the resulting value of α_q was 3.9 $\mu \epsilon / ^{\circ}$ C. Note that a wide range of thermal deformation coefficient values for quartz are reported in the literature, ranging from 0.5 $\mu \epsilon / ^{\circ}$ C for silica (amorphous) [27] to 9.3 $\mu \epsilon / ^{\circ}$ C for quartzite [28].

5.2.4. Mixed inclusion measurements

Fig. 7c plots the experimentally measured effective thermal deformation coefficient α_{eff} of microencapsulated PCM-mortar composite specimens with both PCM and quartz sand inclusions as a function of PCM volume fraction ϕ_{c+s} ranging from 0 to 0.5. Here, the total inclusion volume fraction was kept constant for all specimens such that $\phi_q + \phi_{c+s} = 0.5$. In particular, note that α_{eff} for a specimen with ϕ_c $\phi_{+s} = 0.2$ and $\phi_q = 0.3$ was measured to be 14.0 $\mu \epsilon / C$ while that of the cementitious matrix was measured earlier as $\alpha_m = 14.1 \,\mu\epsilon/^{\circ}$ C. Thus, the effect of adding 20 vol.% microencapsulated PCM was "offset" by the addition of 30 vol.% quartz. Finally, Fig. 7c shows the predictions of α_{eff} by Schapery's model using the values of α_{c+s} and α_{a} retrieved from previous experiments (Fig. 7a-b). Excellent agreement was found between α_{eff} predicted by the Schapery model and measured experimentally. These results demonstrate the ability of Schapery's model to account for the combined, independent effects of both inclusions on the effective thermal deformation coefficient of the mortars.

5.2.5. Design rule for thermal deformation equivalence in PCM-mortar composites

As shown in Fig. 7, the addition of PCM microcapsules tends to increase the effective thermal deformation coefficient of the composite while the addition of quartz sand tends to decrease it. Therefore, one could "compensate" for the increase in α_{eff} caused by the addition of PCM microcapsules by adding an appropriate amount of quartz sand to maintain the ratio α_{eff}/α_m below some threshold. Fig. 8 plots the required quartz sand volume fraction ϕ_q corresponding to a ratio α_{eff}/α_m equal to 1.25, 1, or 0.75, as a function of microencapsulated PCM volume fraction ϕ_{c+s} ranging from 0 to 0.3. Here, Schapery's model was used with the retrieved values of α_{c+s} and α_q to determine ϕ_q for each α_{eff}/α_m and ϕ_{c+s} . Note that for a desired ratio $\alpha_{eff}/\alpha_m < 0.75$, PCM



Fig. 8. Required quartz sand volume fraction ϕ_q to ensure that the ratio α_{eff}/α_m of a PCM-mortar composite remains equal to 1.25, 1, or 0.75, plotted as a function of micro-encapsulated PCM volume fraction ϕ_{c+s} ranging from 0 to 0.3.

volume fractions above ~0.25 are not feasible as they require a minimum total inclusion volume fraction $\phi_{c+s} + \phi_q$ of 0.85 or higher. Also, for an allowable ratio of $\alpha_{eff}/\alpha_m = 1.25$, no quartz sand is required for PCM volume fraction ϕ_{c+s} below 0.125.

6. Conclusion

This paper examined the effect of microencapsulated PCMs and other particulate inclusions on the thermal deformation behavior of cementitious composites, and presented a convenient approach to estimate the thermal deformation coefficient of inclusions based on measured effective properties. The effective thermal deformation coefficient of three-component core-shell-matrix composites was first predicted numerically using finite element simulations of free thermal deformation. It was found to be a function of only the constituents' volume fractions and thermomechanical properties. Predictions from the effective medium approximation developed by Schapery were found to agree well with the numerical results over a wide range of constituent thermal deformation coefficients. Moreover, the effective thermal deformation coefficient of cementitious microencapsulated PCM-composites was measured experimentally for cement paste and cement mortar with various volume fractions of quartz sand and microencapsulated PCM. The experimental measurements were used in conjunction with Schapery's model to retrieve the thermal deformation coefficient of PCM microcapsules and of quartz sand grains. The thermal deformation coefficient of the PCM microcapsules was found to be near that of the shell material, due to the fact that the capsules might not be completely filled with PCM, thus leaving space inside for the PCM core to expand. Schapery's model was shown to predict accurately the effective thermal deformation coefficient of cementitious composite samples with a mixture of microencapsulated PCM and quartz sand inclusions based on the previously retrieved properties. Finally, a design rule was suggested for determining the amount of quartz sand required to offset the effect of the PCM microcapsules in increasing the thermal deformation coefficient of PCM-mortar composites. These results could be useful in modeling the thermal deformation behavior of pavement sections featuring microencapsulated PCMs for crack resistance.

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